

# Current Problems in Material Modeling of Polymers: Glass-Fiber Reinforced Plastics

LS-DYNA Forum, Filderstadt 2013

Stefan Kolling<sup>1</sup>, Andreas Rühl<sup>1</sup>, Manuel Roth<sup>1</sup>, Matthias Vogler<sup>2</sup>, Sebastian Mönnich<sup>3</sup>

<sup>1</sup> Institute of Mechanics and Materials, THM Gießen

<sup>2</sup> Consulting Engineer, [vogler.consulting@email.de](mailto:vogler.consulting@email.de)

<sup>3</sup> Fraunhofer Institute for Structural Durability and System Reliability LBF, Darmstadt

- Generation of input data
- Influence of injection molding process
- Orientation of glass fibers
- Involving anisotropy for fiber reinforced plastics

- 2004: Glaser/Wüst (BASF) present their concept for integrative simulation using micromechanical model.
- 2006: First applications of Glaser's model presented by Frik (Opel).
- 2009: Adams et al. and Seyfarth et al. (e-Xstream) present the LS-DYNA MPP interface of DIGIMAT

- 2010: Nutini / Vitali (LyondellBasell) validate drop tests and three point bending tests using MAT\_103
- 2011: Schöpfer et al. presented a full verification procedure of PAGF. They used a combined MAT\_54 / MAT\_108 model for validation

# Input data generation for polymers (q.s.)

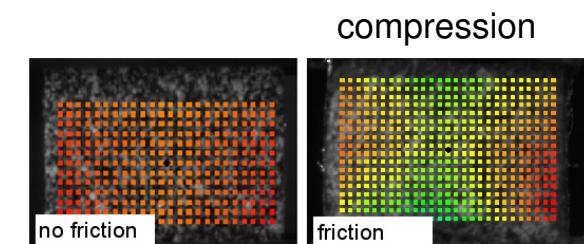
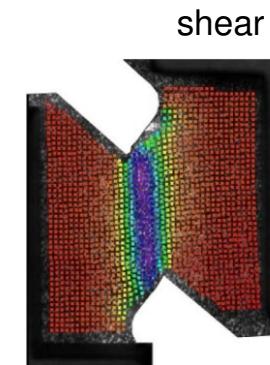
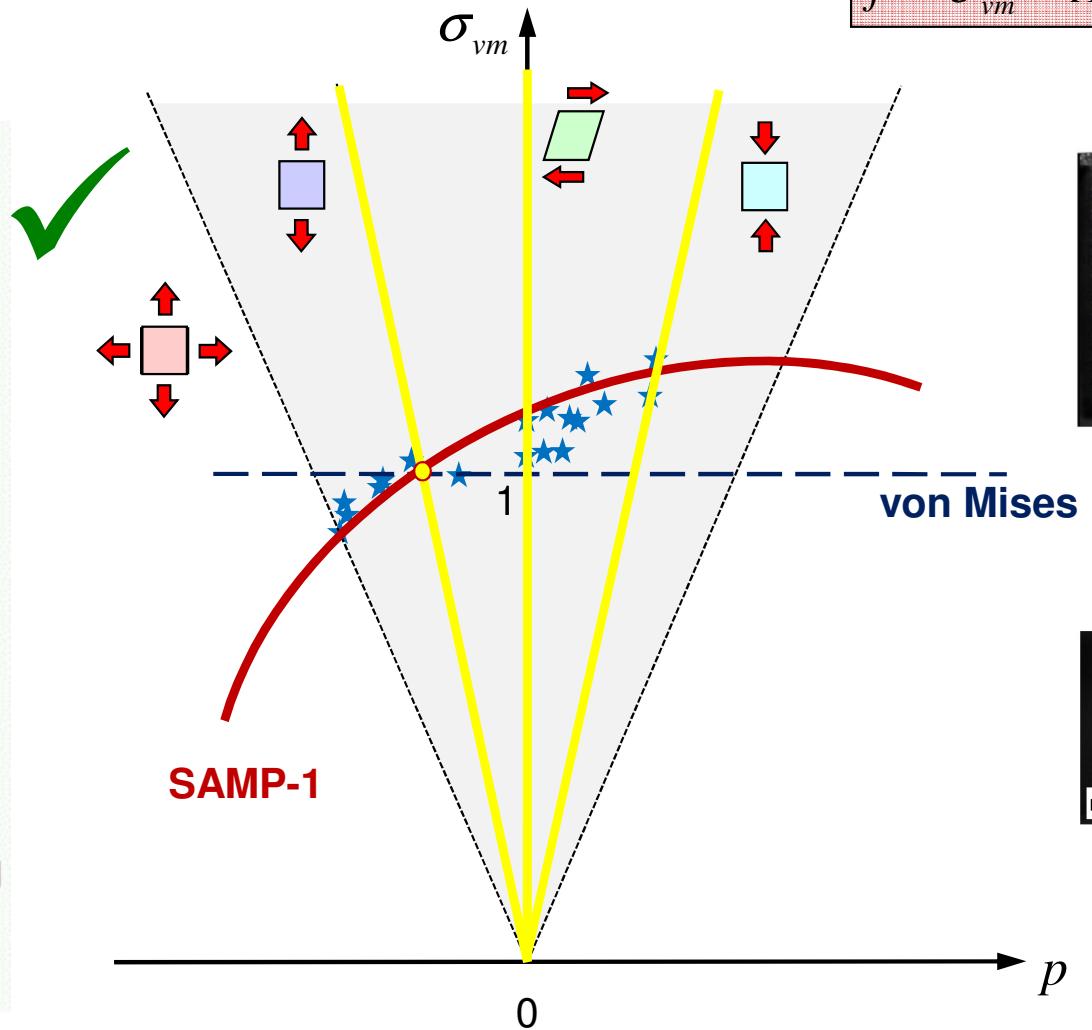
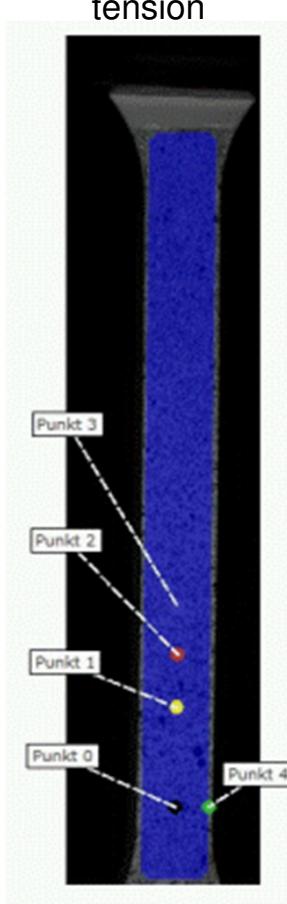


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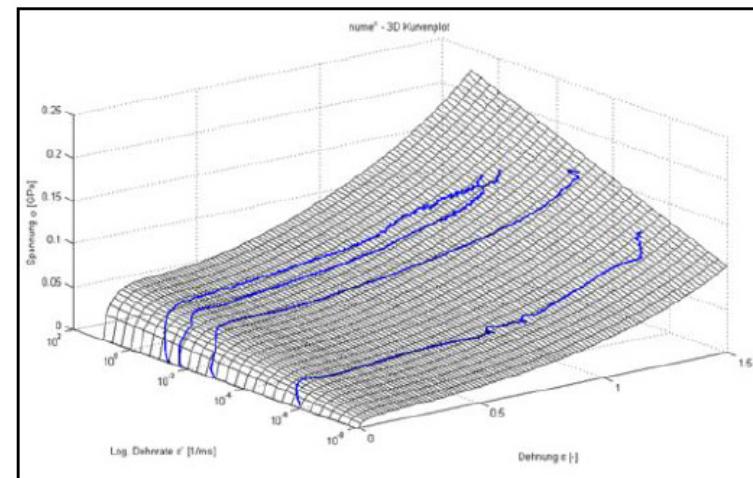
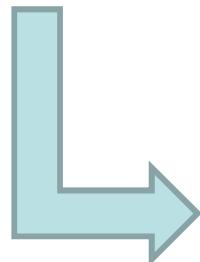
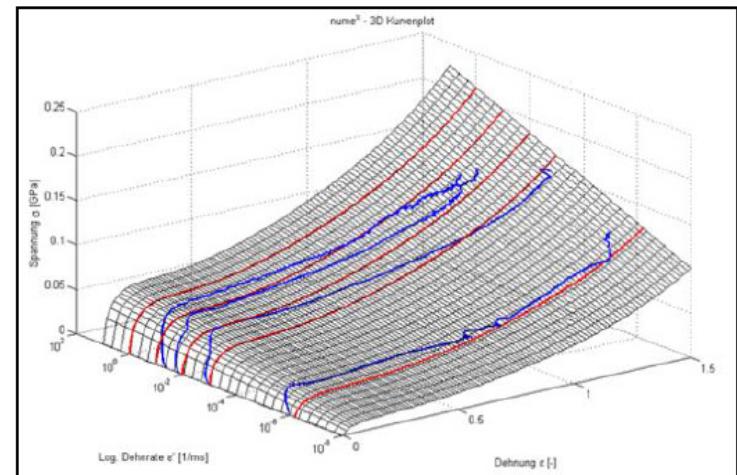
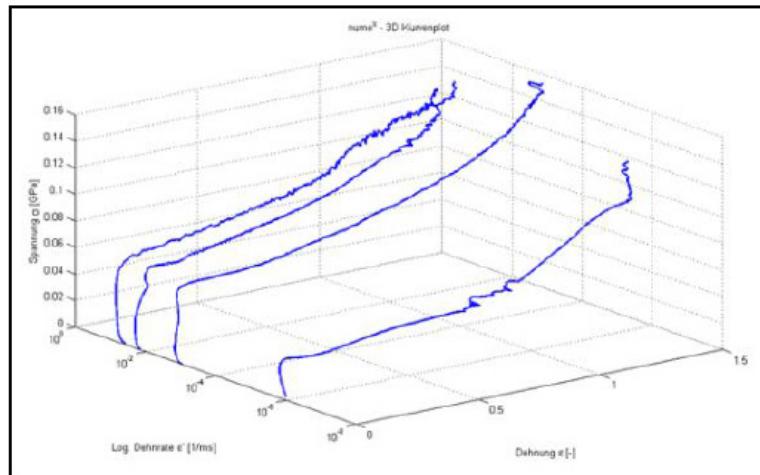
Example: PC (Bardenheier 1982)

$$f = \sigma_{vm}^2 - A_0 - A_1 p - A_2 p^2 \leq 0$$



# Input data generation for polymers (dyn.)

- Strain rate is not constant during tensile tests!

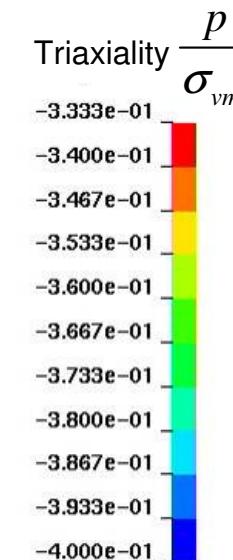
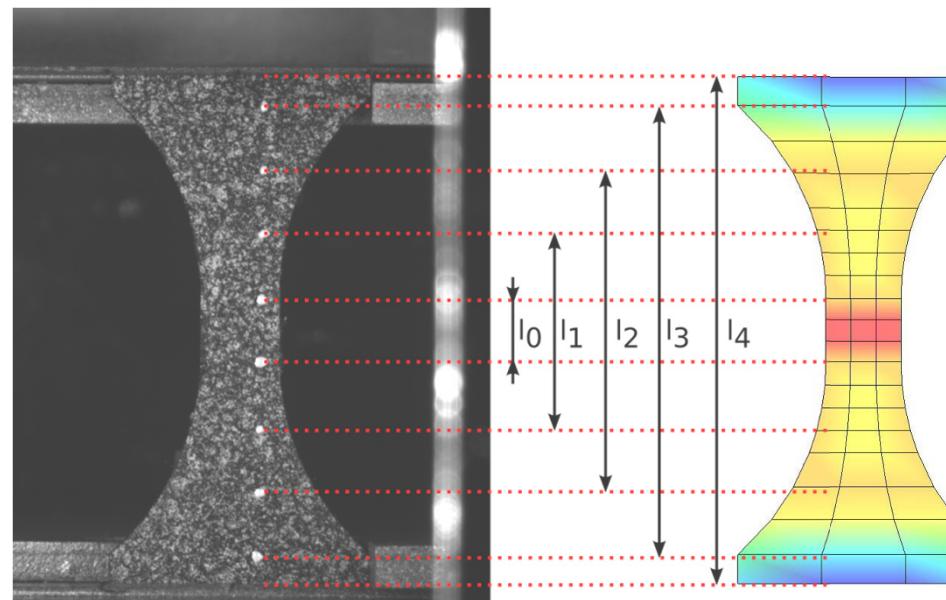


# Reinforced polymers - PA6GF60

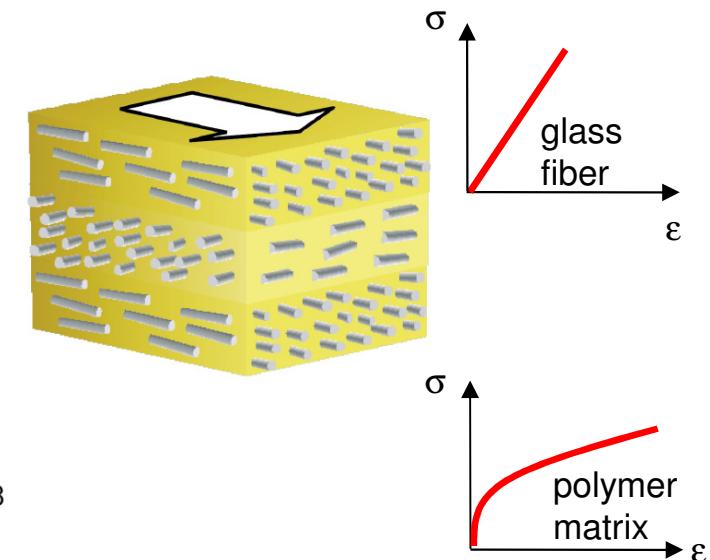
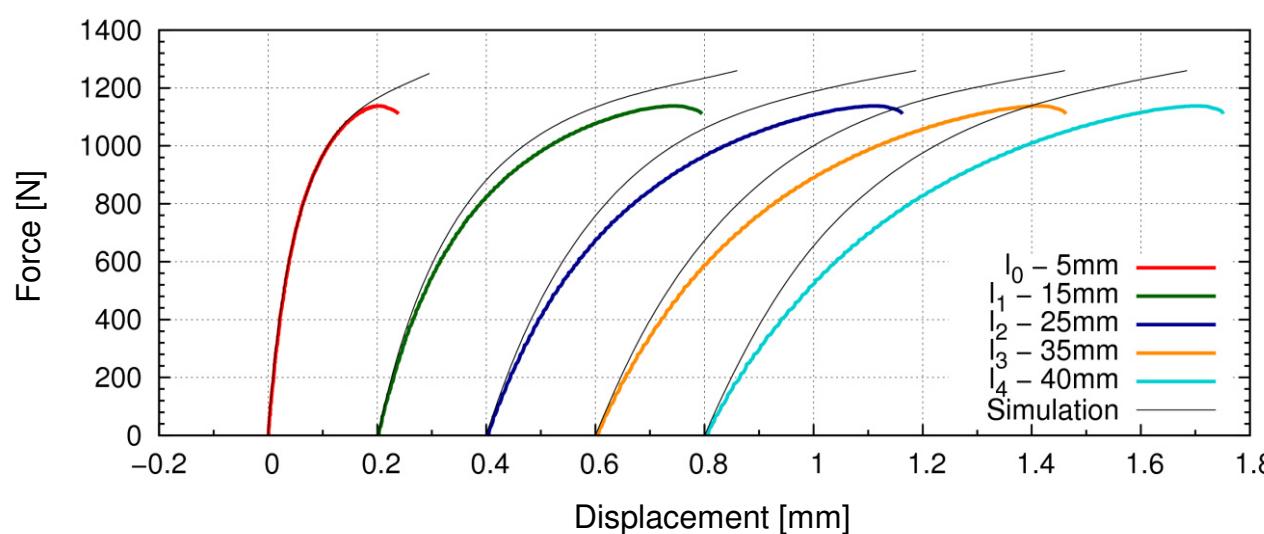
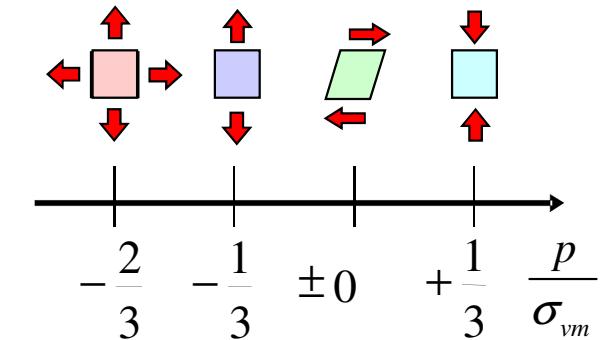


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[J. Schöpfer, Dissertation 2011]



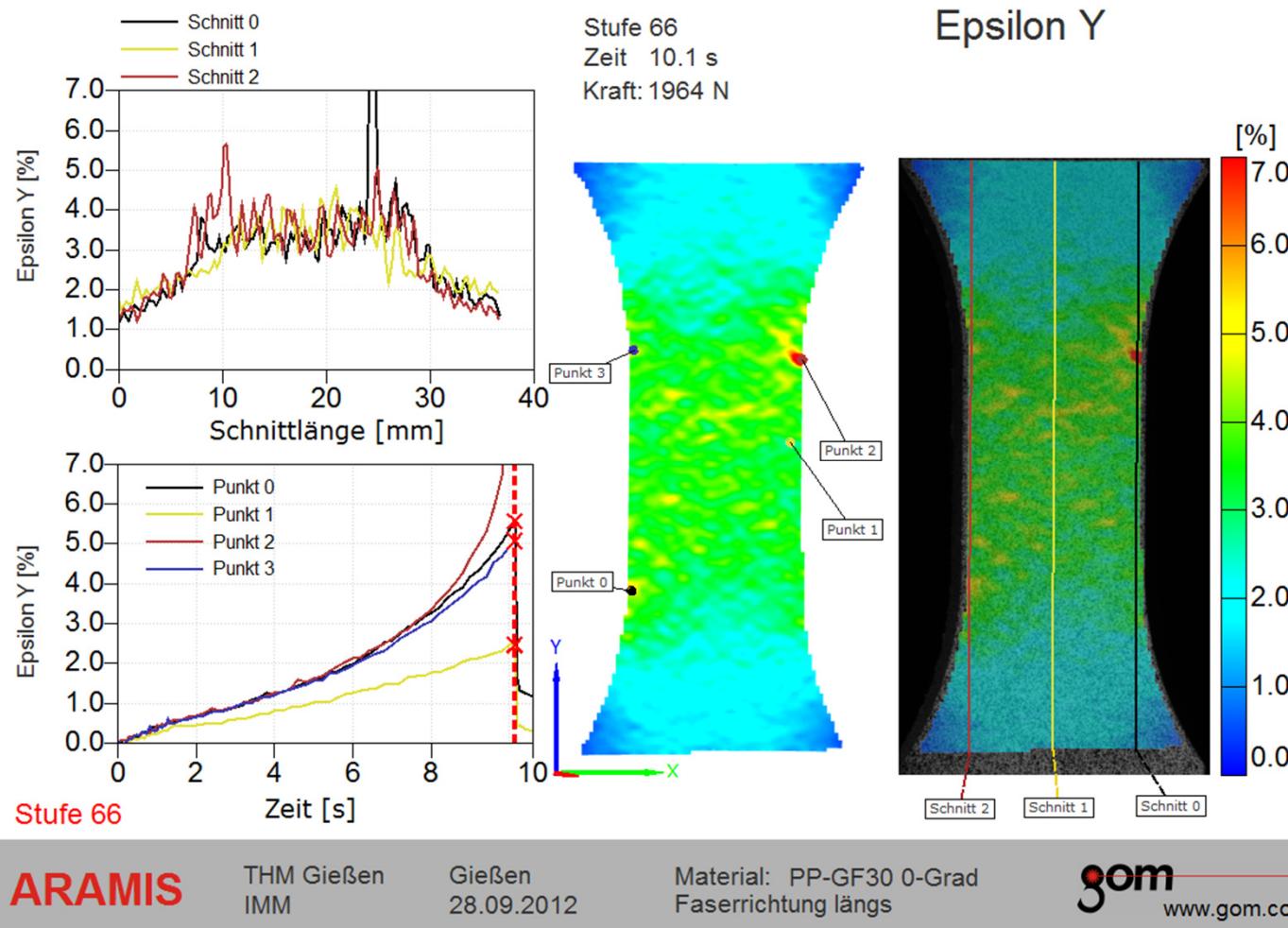
# Strain distribution during tensile test



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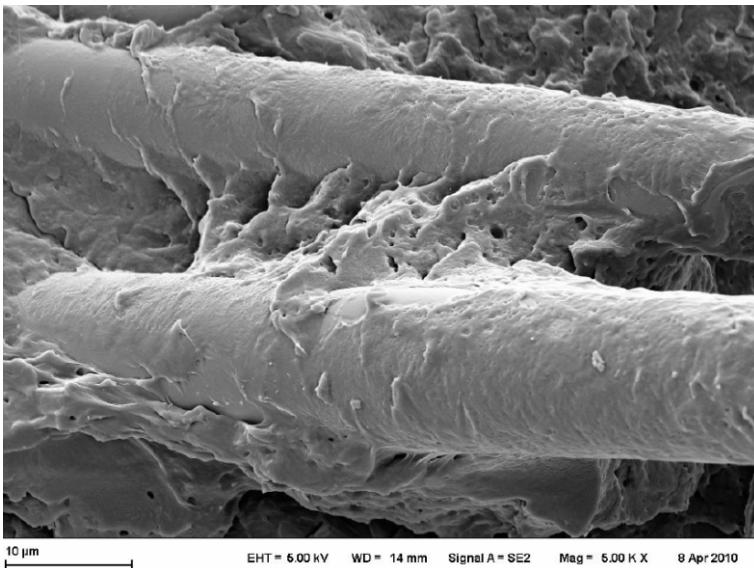
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- Inhomogeneous strain distribution due to local fiber fracture



[J. Schöpfer, Dissertation 2011]

- Local behavior of the fibers is rather complex!



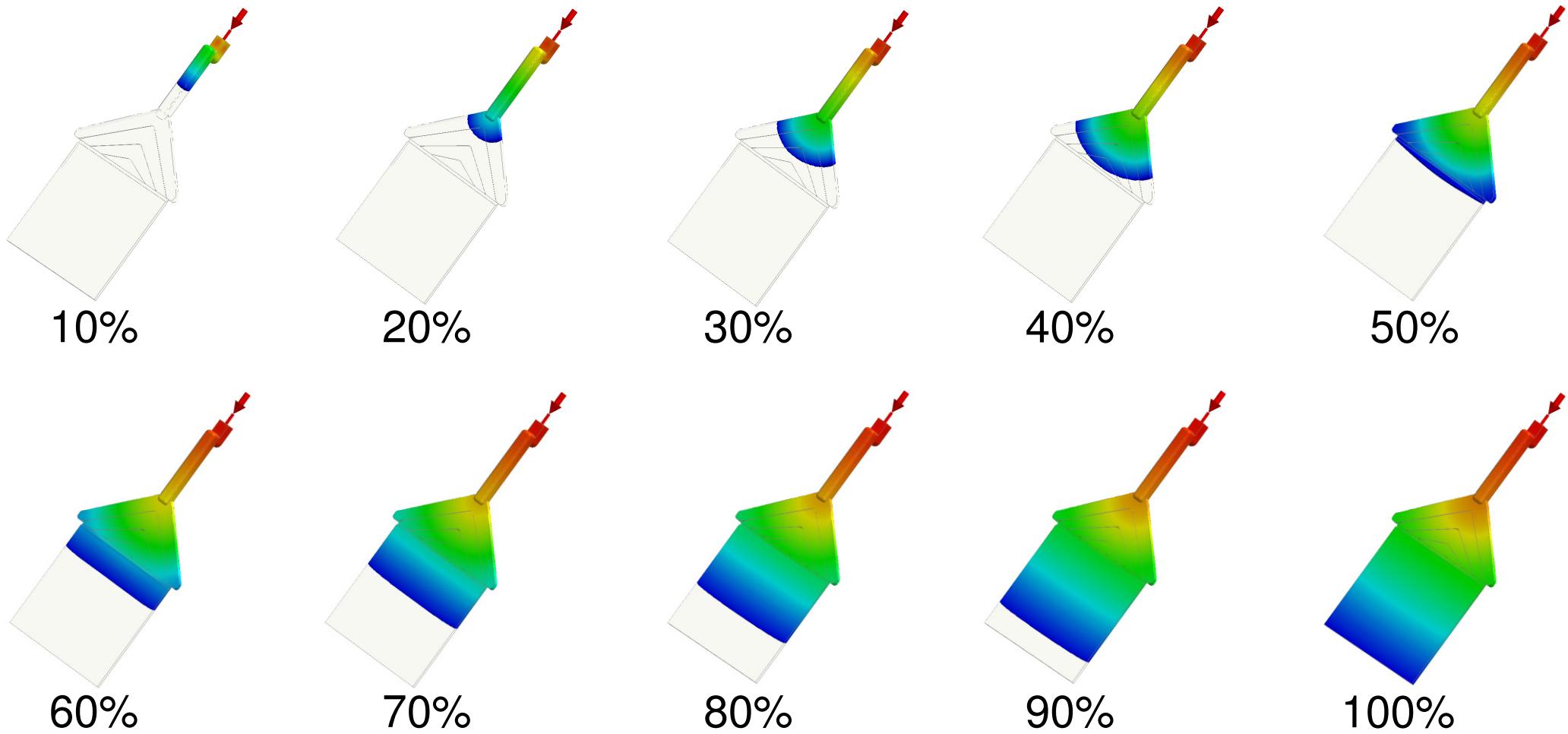
- Fiber distribution can be obtained numerically by injection molding analysis
- Validation of the analysis can be performed by µCT-Analysis

# Injection molding analysis



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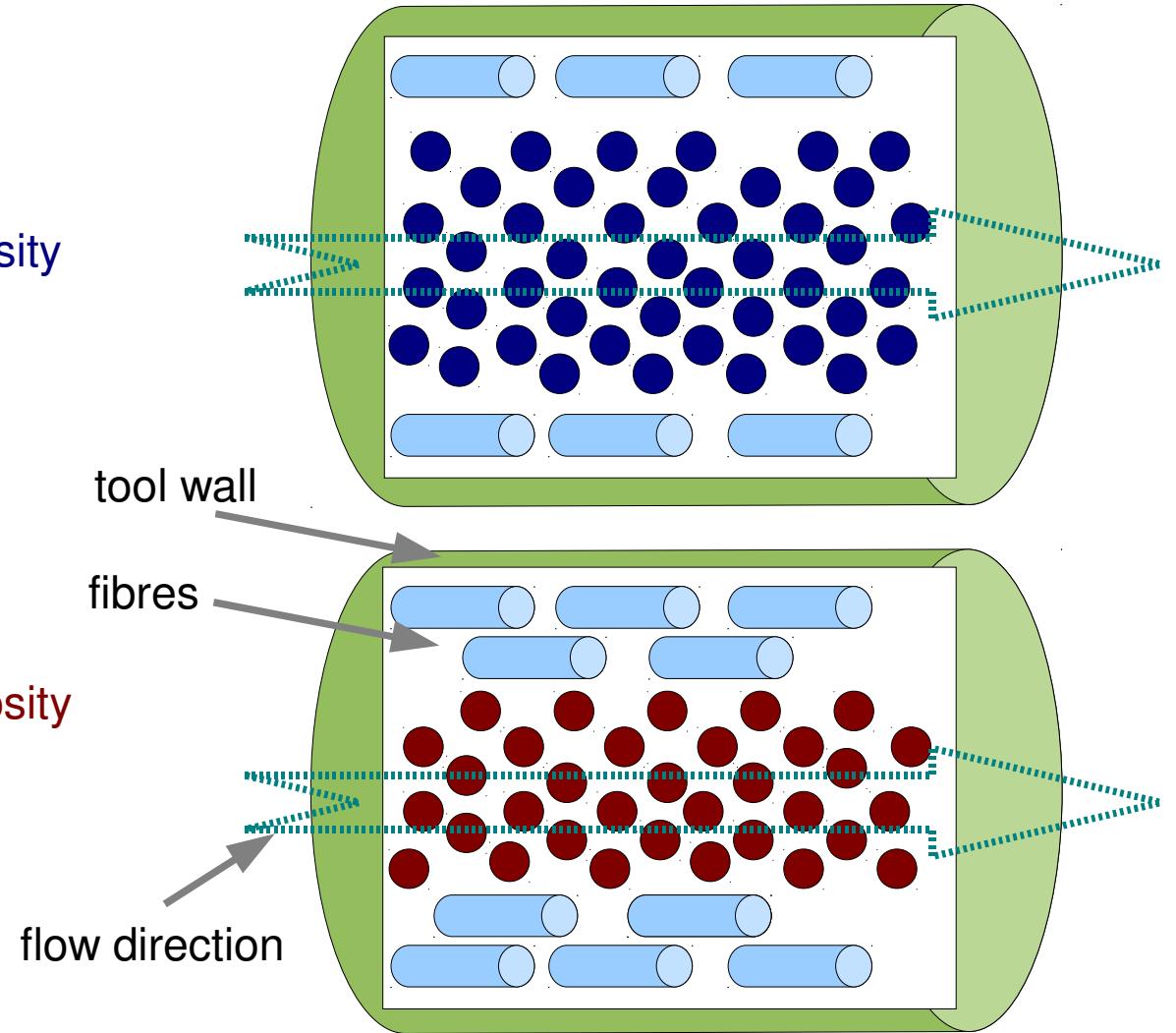
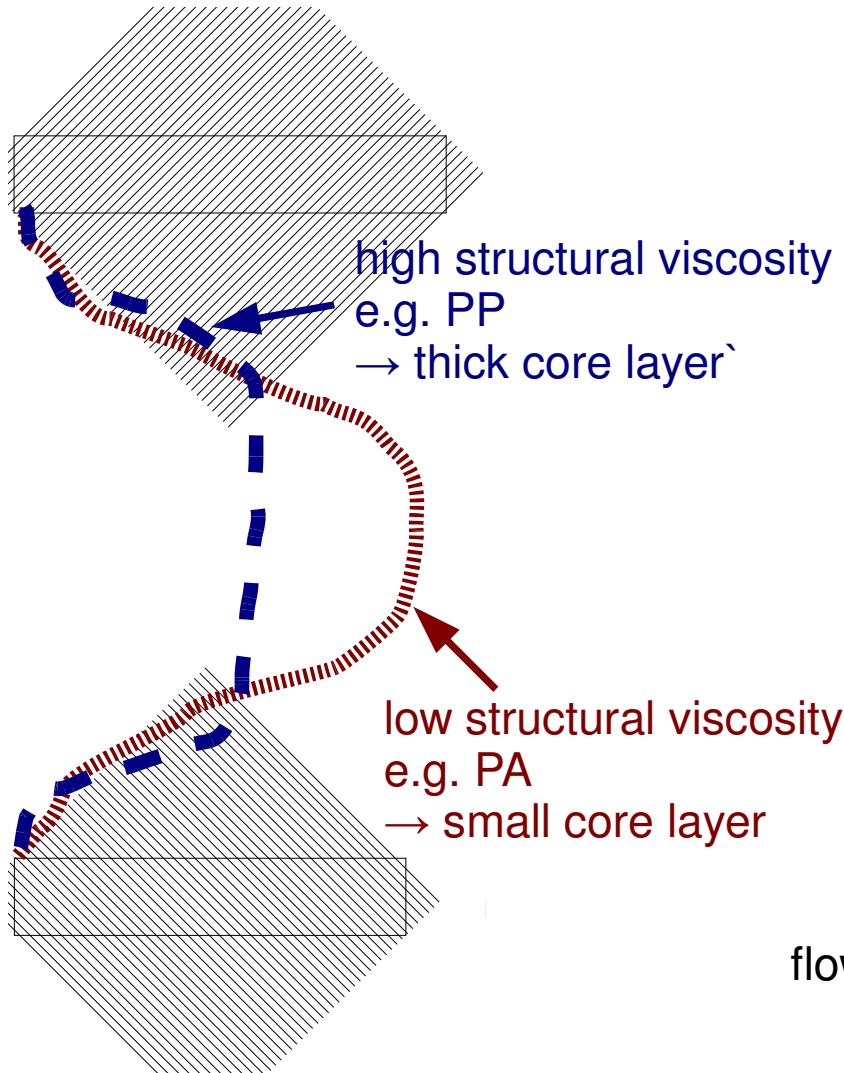


# Fluid flow & fibre orientation

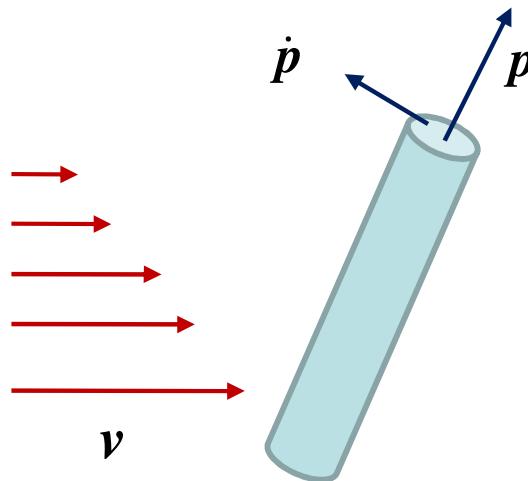


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- Evolution of fiber orientation (Jeffrey 1922, Folgar&Tucker 1984)



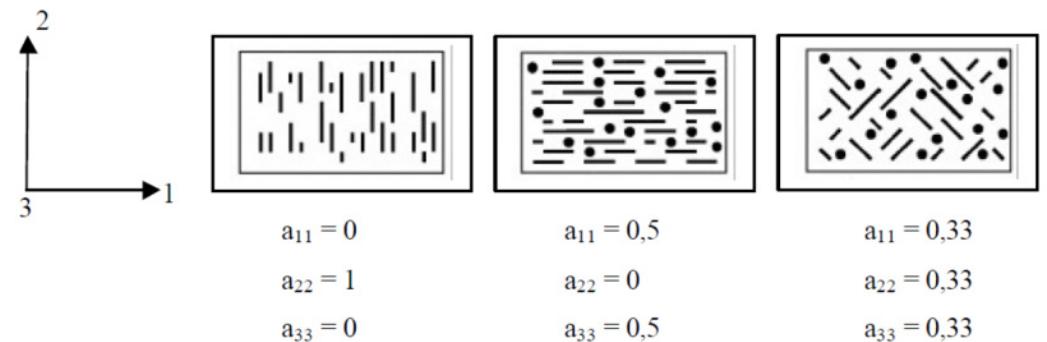
$$\dot{p} = -\nabla^{skew} v \cdot p + \lambda \left[ \nabla^{sym} v \cdot p - (p \cdot \nabla^{sym} v) p \right] - \frac{Dr}{\psi} \frac{\partial \psi}{\partial p}$$

$$\lambda = \frac{(l/d)^2 - 1}{(l/d)^2 + 1} \quad = \text{fiber geometry}$$

$Dr$  = fiber interaction coefficient

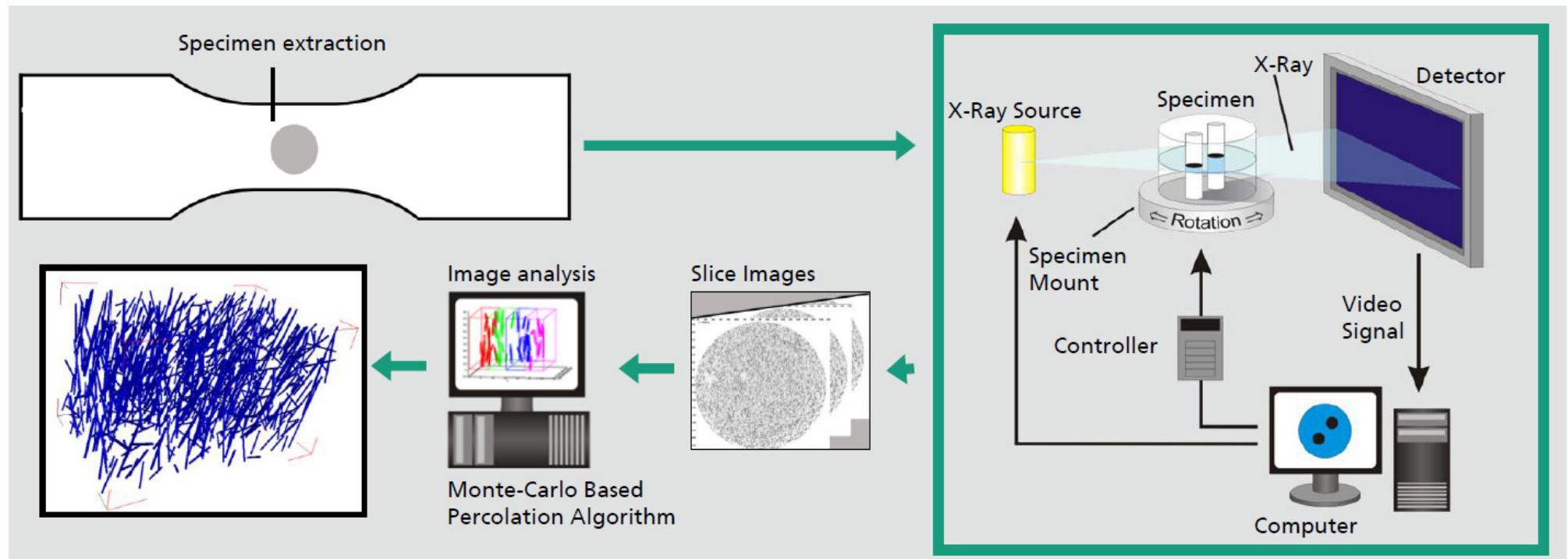
- Fiber orientation tensor

$$a_{ij} = \oint \Psi(\mathbf{p}) p_i p_j d\mathbf{p}$$



# Fiber analysis using computer-tomography

- Experimental fully 3D-identification of the fiber orientation tensor at the Fraunhofer LBF, Darmstadt



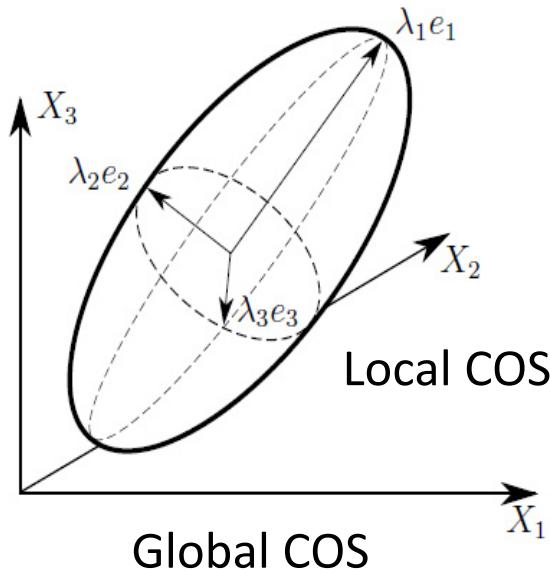
# SAMP-anisotropic including fiber orientation



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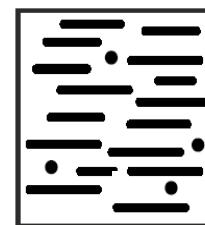
Fiber orientation tensor:



$$a_{11} = 0.80$$

$$a_{22} = 0.20$$

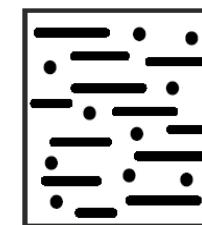
$$a_{33} = 0.00$$



$$a_{11} = 0.60$$

$$a_{22} = 0.40$$

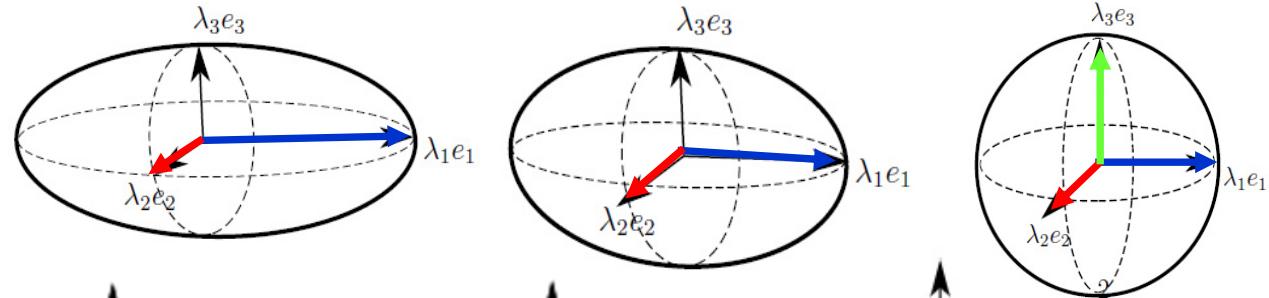
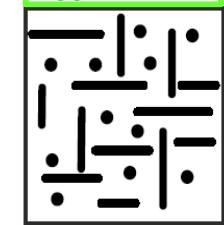
$$a_{33} = 0.00$$



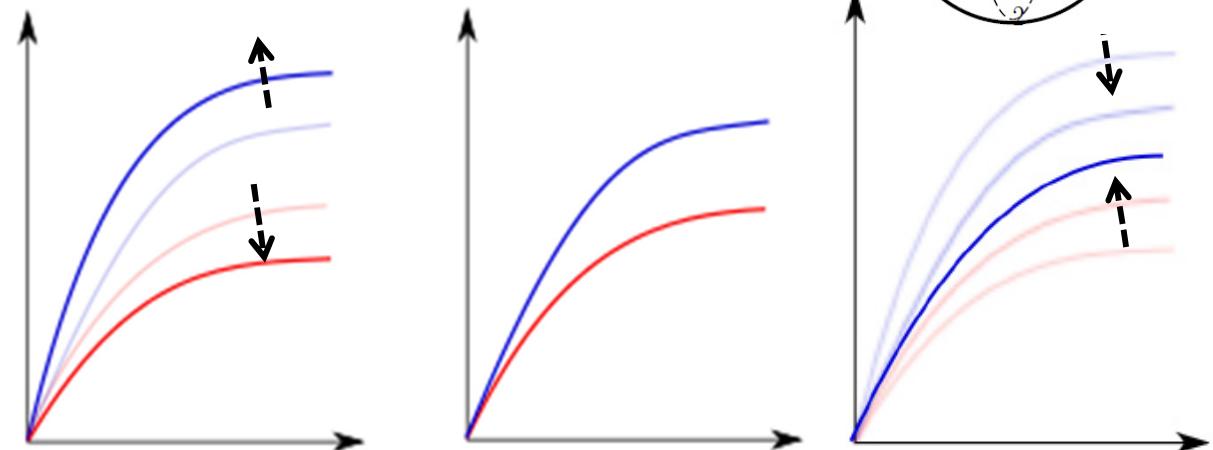
$$a_{11} = 0.33$$

$$a_{22} = 0.33$$

$$a_{33} = 0.33$$

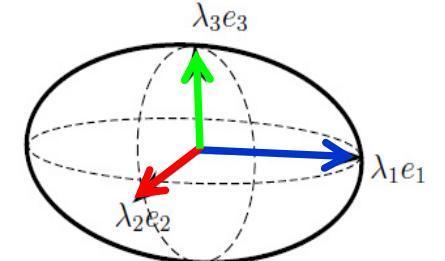


Tensile behavior :



# SAMP anisotropic: Yield surface formulation

- Structural tensors:  $A = a \otimes a$  A = a  $\otimes$  a    $B = b \otimes b$  B = b  $\otimes$  b
- Decomposition of stress tensor  $\sigma = \sigma^{\text{pind}} + \sigma^{\text{reac}}$  in reaction stress tensor and plasticity inducing stresses
- Orthotropic invariants



$$\begin{aligned} I_1 &:= \frac{1}{2} \operatorname{tr} (\sigma^{\text{pind}})^2 - a (\sigma^{\text{pind}})^2 a - b (\sigma^{\text{pind}})^2 b & I_4 &:= \operatorname{tr} \sigma - a \sigma a - b \sigma b \\ I_2 &:= a (\sigma^{\text{pind}})^2 a, & I_5 &:= \frac{3}{2} a \sigma^{\text{dev}} a, \\ I_3 &:= b (\sigma^{\text{pind}})^2 b. & I_6 &:= \frac{3}{2} b \sigma^{\text{dev}} b \end{aligned}$$

- Orthotropic yield surface formulation

$$f = \alpha I_1 + \beta I_2 + \gamma I_3 + \delta I_5^2 + \epsilon I_6^2 + \zeta I_5 I_6 + \eta I_4^2 + \theta I_4 I_5 + \iota I_4 I_6 - 1$$

9 yield parameters  $\longrightarrow$  9 material tests necessary

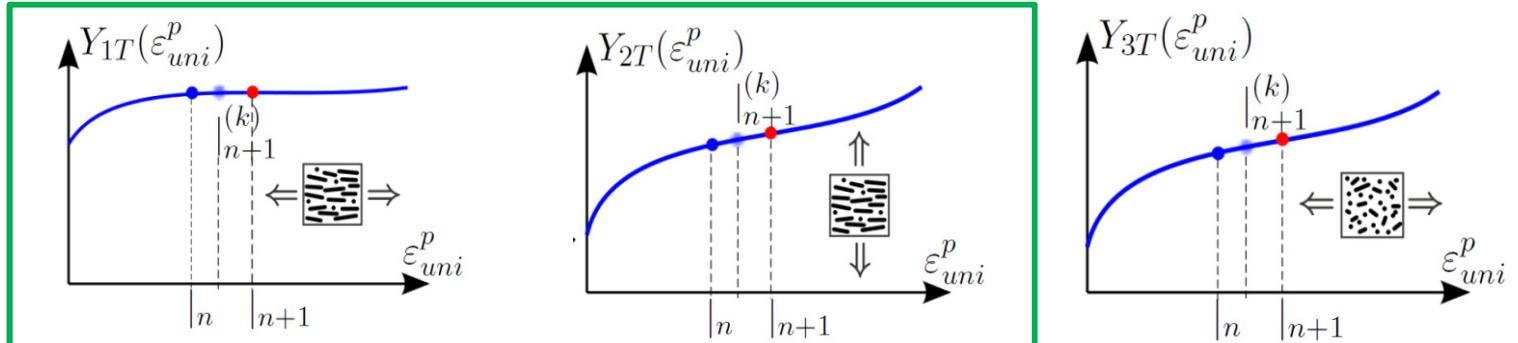
# SAMP anisotropic: Different yielding in..



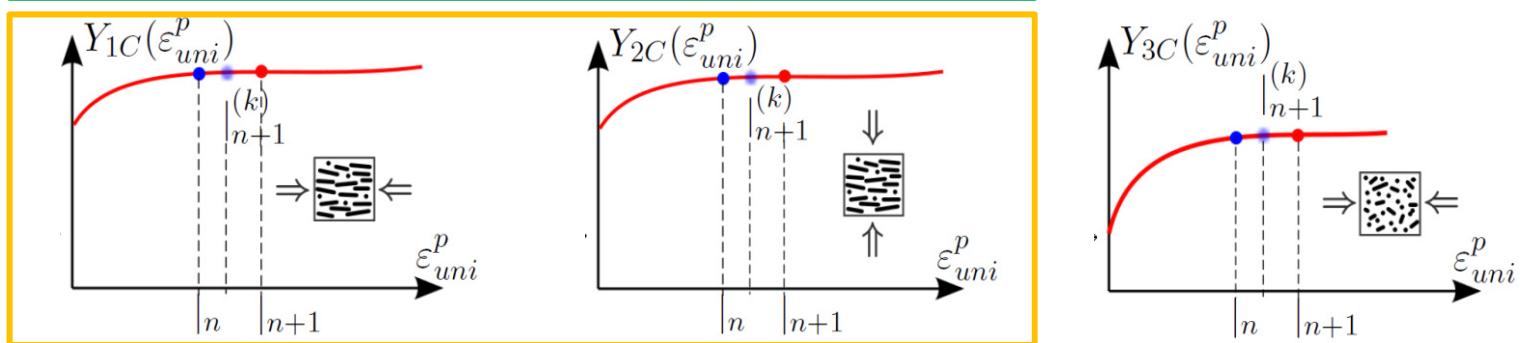
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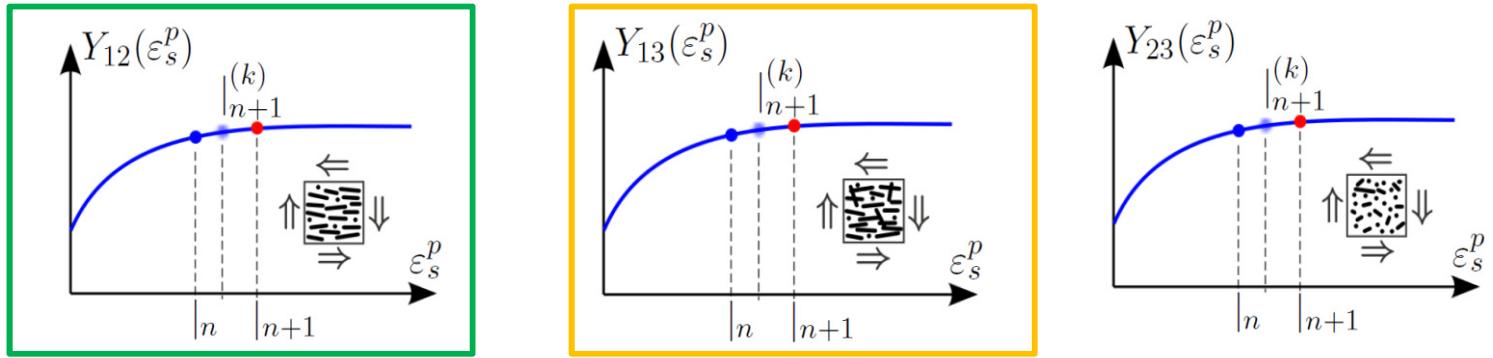
.. tension:



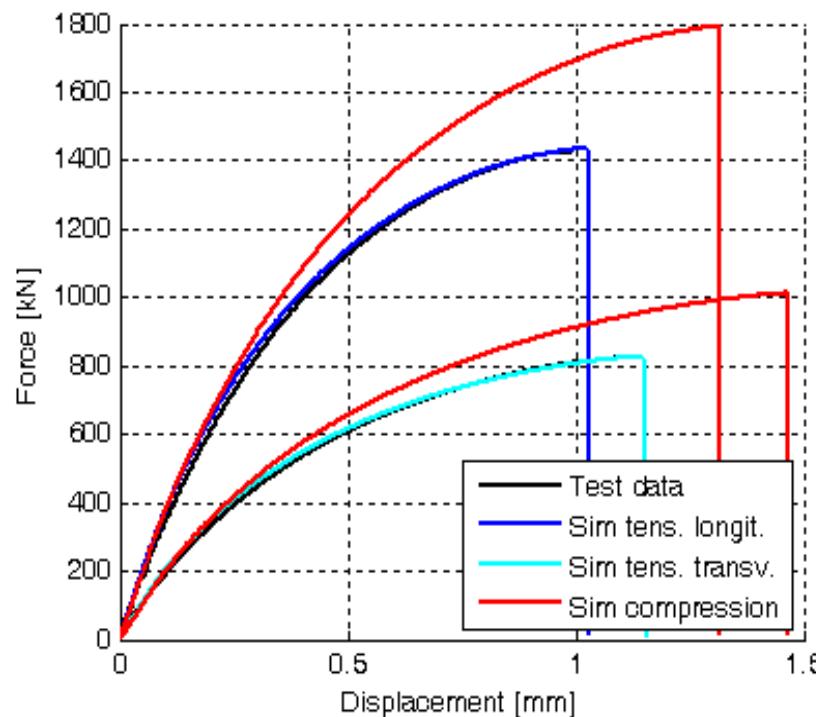
.. compression:



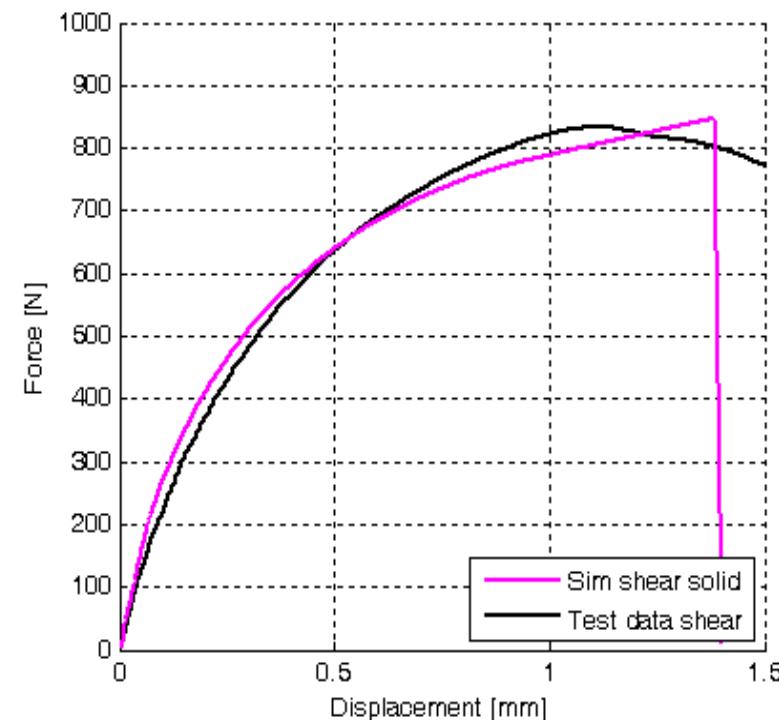
.. shear:



## Tension and compression



## Shear



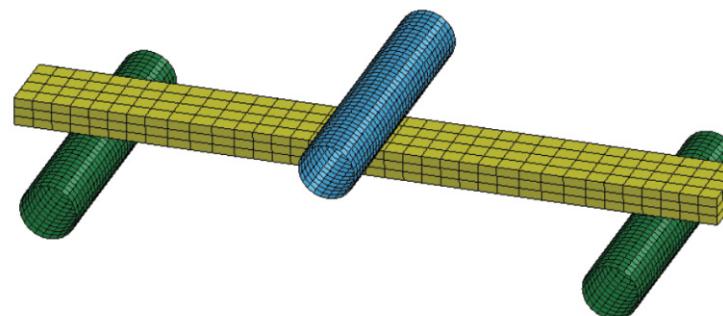
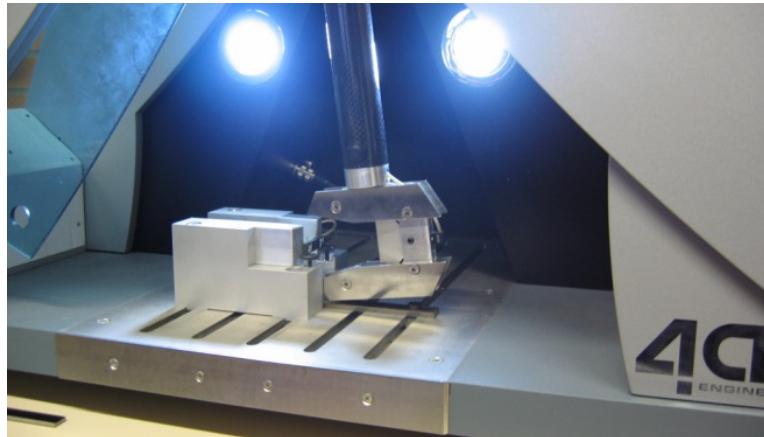
- Note that there is no test data available under compression. The tension-compression asymmetry has been obtained via three-point-bending tests by reverse engineering

# PA6GF60: Simulation results 3-point bending tests

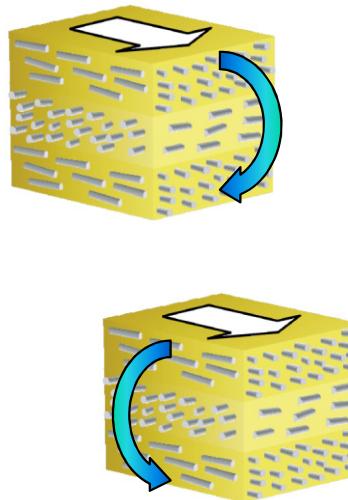
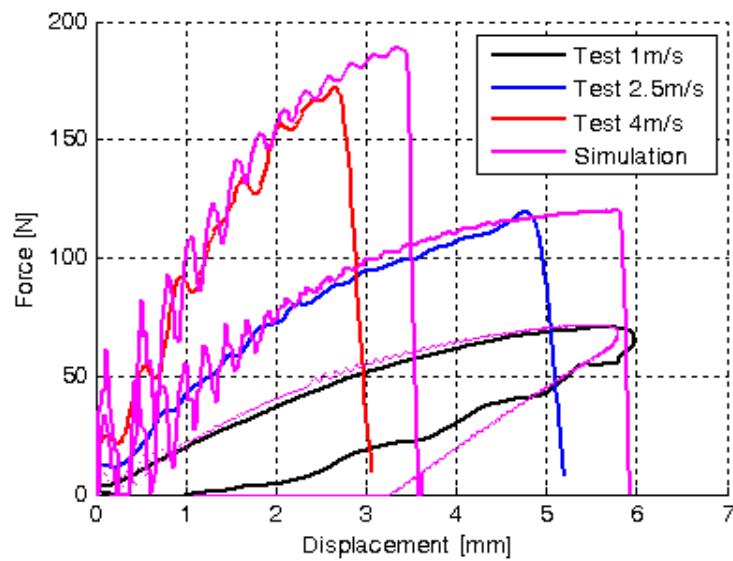


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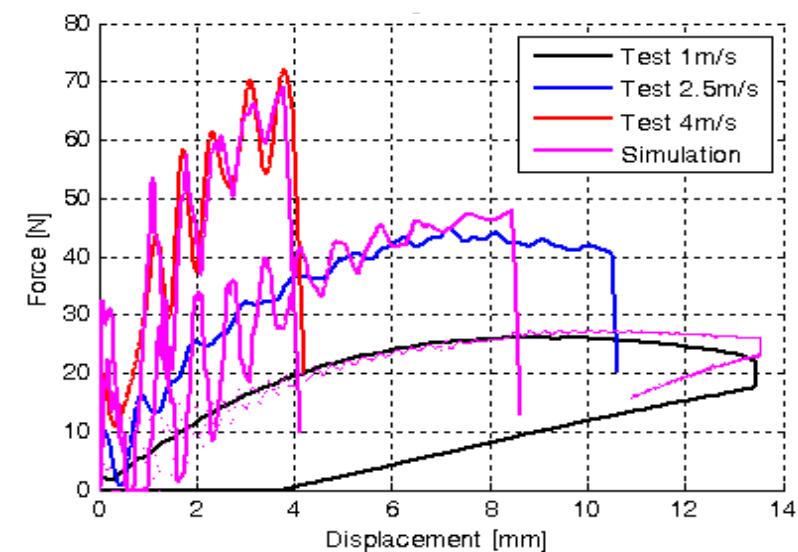
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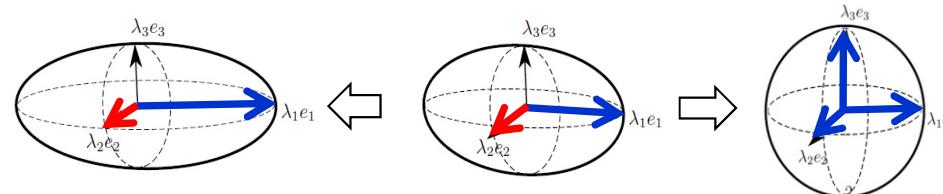
Longitudinal fiber orientation



Transverse fiber orientation



- Based on MAT\_SAMP-1, an anisotropic version of this model has been implemented into LS-DYNA
- Information of the fiber orientation tensor is required at Gauss points
- Extrapolation / interpolation to arbitrary fiber orientations using micromechanics



- Consideration of the process chain from injection molding simulation to crash simulation becomes feasible without further external codes
- Validation of component tests (Nutini's box tests) are next steps